1052. The Structure of Chimonanthine: X-Ray Analysis of Chimonanthine Dihydrobromide¹

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Chimonanthine, $C_{22}H_{26}N_4$, an alkaloid from *Chimonanthus fragrans*, has been shown to have structure (III; R = R' = H) by X-ray analysis of the dihydrobromide. Crystals of the dihydrobromide belong to the tetragonal system, space group $P4_12_12$ (or the enantiomorphous $P4_32_12$), with eight molecules of $C_{22}H_{28}Br_2N_4$ in the unit cell of dimensions a = b = 13.95, c =26.67 Å. Several three-dimensional electron-density distributions were evaluated and followed by least-squares refinement of the atomic coordinates. The final discrepancy R over 2093 independent reflexions is 14·9%.

FROM Chimonanthus fragrans, the deciduous shrub commonly known as Winter Sweet, Hodson, Robinson, and Smith² isolated an alkaloid chimonanthine, $C_{22}H_{26}N_4$, isomeric with calycanthine (I).³ The ultraviolet spectrum of the alkaloid indicated the presence of the grouping Ph·N·C·N, and reduction with zinc and hydrochloric acid yielded 3-2'methylaminoethylindoline showing that, like calcyanthine, the alkaloid contains two tryptamine units. In contrast to calycanthine, chimonanthine on zinc dehydrogenation

¹ For a preliminary report see I. J. Grant, T. A. Hamor, J. M. Robertson, and G. A. Sim, Proc.

<sup>Chem. Soc., 1962, 148.
² H. F. Hodson, B. Robinson, and G. F. Smith, Proc. Chem. Soc., 1961, 465.
³ Sir R. Robinson and H. J. Teuber, Chem. and Ind., 1954, 783; T. A. Hamor, J. M. Robertson, H. N. Shrivastava, and J. V. Silverton, Proc. Chem. Soc., 1960, 78; R. B. Woodward, N. C. Yang, T. J. Katz, V. M. Clark, J. Harley-Mason, R. F. J. Ingleby, and N. Sheppard,</sup> *ibid.*, p. 76.

gave only traces of calycanine (II). Chimonanthine has aromatic NH groups and aliphatic tertiary N-methyl groups. The structural possibilities were narrowed to two formulæ (III; R = R' = H) and (IV) which were not readily distinguished chemically.



At the suggestion of Dr. G. F. Smith we undertook an X-ray crystal-structure analysis of chimonanthine dihydrobromide in order to provide an unambiguous determination of the molecular structure. Our results establish structure (V) for the dihydrobromide so that chimonanthine has therefore to be assigned structure (III; R = R' = H). Saxton, Bardsley, and Smith⁴ have shown that two other naturally occurring alkaloids, calycanthidine and folicanthine, represent successive further stages of methylation of chimonanthine; it follows that calycanthidine must be formulated as (III; R = H, R' = Me) and folicanthine as (III; R = R' = Me).

The crystal structure was solved by means of the usual phase-determining heavy-atom method.⁵ Four three-dimensional electron-density distributions were calculated and the positional and thermal atomic parameters were then further improved by the method of

Table	1
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Atomic co-ordinates (origin of co-ordinates as in "International Tables for X-Ray Crystallography," The Kynoch Press, Birmingham, 1952, vol. I)

Atom	x a	y/b	z/c	Atom	x a	y/b	z/c
C(1)	0.7967	0.4854	0.4351	C(4')	0.8641	0.4812	0.5988
C(2)	0.7670	0.5813	0.4280	C(5')	0.8582	0.4132	0.5578
C(3)	0.6668	0.6023	0.4330	C(7')	0.9096	0.3051	0.5048
C(4)	0.6007	0.5361	0.4435	C(9')	0.8899	0.1697	0.5449
C(5)	0.6302	0.4449	0.4527	C(10')	0.7932	0.1830	0.5187
C(7)	0·6303	0.2788	0.4689	C(11')	0.8022	0.2895	0.5057
C(9)	0.6774	0.2363	0.3850	C(12')	0.7815	0.3584	0.5487
C(10)	0.7690	0.2581	0.4115	C(13')	0.0587	0.2324	0.5380
C(11)	0.7340	0.3136	0.4600	N(6)	0.5710	0.3692	0.4647
C(12)	0.7232	0.4192	0.4479	N(8)	0.6039	0.2065	0.4268
C(13)	0.5073	0.1977	0.4127	N(6')	0.9423	0.3873	0.5262
C(1')	0.7016	0.3649	0.5779	N(8')	0 ·9607	0.2134	0.5122
C(2')	0.6986	0.4311	0.6161	Br(I)	0.4868	0.1069	0.5537
C(3')	0.7823	0.4912	0.6248	Br(II)	0.9715	0.0758	0.4173

least-squares. The average discrepancy between measured and calculated structure amplitudes, R, decreased to a final value of 14.9% over 2093 independent reflexions.

⁴ J. E. Saxton, W. G. Bardsley, and G. F. Smith, *Proc. Chem. Soc.*, 1962, 148. ⁵ J. M. Robertson and I. Woodward, *J.*, 1937, 219; 1940, 36; G. A. Sim, in "Computing Methods and the Phase Problem in X-ray Crystal Analysis," ed. R. Pepinsky, J. M. Robertson, and J. C. Speakman, Pergamon Press, Oxford, 1961, p. 227.

The third electron-density distribution is shown in Figure 1 as superimposed contour sections drawn parallel to (001) and covering the region of one molecule. The atomic arrangement corresponding to this electron-density distribution is explained in Figure 2. It will be noted that, in the crystal, the molecule is much closer to the *cis*- than to the



FIGURE 1. The third three-dimensional electron-density distribution for chimonanthine dihydrobromide shown by means of superimposed contour sections drawn parallel to (001). Contour interval leÅ⁻³, starting at the 2electron contour

trans-conformation indicated in (V). The final atomic co-ordinates are listed in Table 1 and the interatomic distances and valency angles calculated from the co-ordinates in Table 2. The standard deviations of the final atomic co-ordinates were estimated in the usual manner from the least-squares residuals (see Experimental section) and are shown in





Table 3; from the results the average estimated standard deviation (e.s.d.) of a carboncarbon bond length is about 0.08 Å and the average e.s.d. of a valency angle about 4° .

The average bond length in the benzene ring, 1.39 Å, and the average carbon-carbon single bond length, 1.54 Å, agree well with the accepted values of 1.397 and 1.545 Å 6 for such bonds. The average $C(sp^3)$ -N⁺ bond length of 1.50 Å is in reasonable agreement with the lengths of such bonds in other alkaloids, e.g., 1.49 Å in macusine-A iodide, 7 1.54 Å in echitamine bromide.8

In the five-membered rings B and B' the average valency angle is 108° whereas in the five-membered rings c and c' the corresponding value is only 104°. A similar difference exists in the echitamine molecule.⁸ In saturated five-membered rings the average valency

TABLE 2

Interatomic distances (Å) and angles

Intramolecular bonded distances

$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccc} 1\cdot54 & C(1')\\ 1\cdot52 & C(2')\\ 1\cdot55 & C(3')\\ 1\cdot57 & C(4')\\ 1\cdot57 & C(5')\\ 1\cdot58 & C(12)\\ 1\cdot58 & C(12)\\ 1\cdot41 & C(5')\\ N(6') \end{array}$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$ \begin{array}{r} 1 \cdot 38 \\ 1 \cdot 44 \\ 1 \cdot 34 \\ 1 \cdot 45 \\ 1 \cdot 34 \\ 1 \cdot 36 \\ 1 \cdot 49 \\ 1 \cdot 36 \\ 1 \cdot 49 \\ 1 \cdot 36 \\ \end{array} $	$\begin{array}{c} C(7')-C(11') \ldots \ldots \\ C(11')-C(12') \ldots \\ C(7')-N(8') \ldots \ldots \\ N(8')-C(9') \ldots \ldots \\ C(9')-C(10') \ldots \ldots \\ C(10')-C(11') \ldots \\ N(8')-C(13') \ldots \ldots \\ C(11)-C(11') \ldots \end{array}$	1.51 1.52 1.48 1.45 1.53 1.53 1.55 1.58
	Intramolecula	r non-bonded d	listances $< 4 \cdot$	0 Å		
$\begin{array}{llllllllllllllllllllllllllllllllllll$	$\begin{array}{c} C(11) \cdots C(13) \\ C(1) \cdots C(5') \\ C(1) \cdots C(7') \\ C(1) \cdots C(1') \\ C(1) \cdots C(1') \\ C(5) \cdots C(1') \\ N(6) \cdots C(1') \\ N(8) \cdots C(10') \\ C(7) \cdots C(10') \\ N(8) \cdots C(10') \\ N(8) \cdots C(10') \\ N(8) \cdots C(10') \\ \end{array}$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	3.64 3.59 3.89 3.25 3.83 3.74 3.57 3.75 3.36 3.44 3.49 3.80 3.16 3.53 2.72 3.36 3.04 3.80	$\begin{array}{c} C(11')\cdots C(13')\\ C(9) \cdots C(11')\\ C(10)\cdots N(8')\\ C(10)\cdots C(1')\\ C(10)\cdots C(1')\\ C(10)\cdots C(1')\\ C(10)\cdots C(1')\\ C(11)\cdots C(1')\\ C(11)\cdots N(6')\\ C(11)\cdots N(6')\\ C(11)\cdots N(8')\\ C(11)\cdots C(9')\\ C(12)\cdots C(1')\\ C(12)\cdots C(5')\\ C(12)\cdots C(7')\\ C(12)\cdots C(1')\\ \end{array}$	3.77 3.74 3.84 3.24 3.06 3.26 3.26 3.42 3.55 3.73 3.55 3.73 3.56 3.48 3.48 3.73 3.41 3.92 2.93
	Intermo	lecular distanc	es < 4.0 Å			
$\begin{array}{c} C(7) \cdots Br(I) \\ N(8) \cdots Br(I) \\ C(10) \cdots Br(II) \\ C(13) \cdots Br(I) \\ N(8') \cdots Br(II) \\ C(9') \cdots Br(II) \\ C(9') \cdots Br(II) \\ C(10') \cdots Br(II) \\ C(2) \cdots C(3') (i) \\ C(2) \cdots C(4') (i) \\ C(2) \cdots C(5') (i) \\ \end{array}$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	3.82 3.68 3.93 3.92 3.77 3.77 3.77 3.80 3.27 3.76	$\begin{array}{l} C(4) \cdots \\ N(6') \cdots \\ Br(II) \cdots \\ C(10) \cdots \\ Br(II) \end{array}$	$\begin{array}{c} C(2') \ (iii) \dots \\ \cdot Br(I) \ (iv) \dots \\ \cdot C(13') \ (v) \dots \\ \cdot C(13') \ (vi) \dots \\ \cdot C(13) \ (vii) \dots \\ \cdot C(13) \ (vii) \dots \\ \cdot C(5) \ (vii) \dots \\ \cdot C(5) \ (vii) \dots \\ \cdot C(13) \ (vii) \dots \\ \cdot C(13) \ (vii) \dots \end{array}$	3.64 3.43 3.84 3.76 3.92 3.80 3.90 3.86 3.85

The figures in parentheses refer to the following equivalent positions.

(i) $\frac{1}{2} + y$,	$\frac{3}{2} - x, -\frac{1}{4} + z;$	(v) $1 + y$, $-1 + x$, $1 - z$;
(ii) $\frac{1}{2} + y$, (iii) y .	$\frac{1}{2} - x, -\frac{1}{4} + z;$	(vi) $\frac{1}{2} - x, -\frac{1}{2} + y, \frac{1}{4} - z;$ (vii) $\frac{1}{4} + x, \frac{1}{4} - y, \frac{3}{4} - z.$
(iv) $1 + y$,	x, 1-z;	

L. E. Sutton et al., "Tables of Interatomic Distances and Configuration in Molecules and Ions," Chem. Soc. Special Publ., No. 11, 1958.
A. T. McPhail, J. M. Robertson, and G. A. Sim, J., 1963, 1832.
J. A. Hamilton, T. A. Hamor, J. M. Robertson, and G. A. Sim, J., 1962, 5061.

TABLE 2 (Continued)

Valency angles

C(12')-C(1')-C(2')

 $\begin{array}{c} C(1') - C(2') - C(3') & \dots \\ C(2') - C(3') - C(4') & \dots \\ C(3') - C(4') - C(5') & \dots \\ \end{array}$

 $C(4') - C(5') - C(12') \dots$

 $\tilde{C}(\tilde{5}') - \tilde{C}(\tilde{1}2') - \tilde{C}(1')$

C(12') - C(11') - C(7')

C(7')-N(6')-C(5') N(6')-C(5')-C(12')

C(9') - N(8') - C(7')'.....

 $\begin{array}{c} C(1') - C(12') - C(11') \\ C(4') - C(5') - N(6') \\ N(6') - C(7') - N(8') \\ C(12') - C(11') - C(11) \\ C(12') - C(11') - C(11) \\ C(11') - C(11') \\ C(11'$

C(10')-C(11')-C(11)

C(7')-C(11')-C(11) C(12')-C(11')-C(10')

C(11') - C(7') - N(6')

C(5')-C(12')-C(11')

C(11')-C(10')-C(9')

 $C(10') - C(9') - N(8')^{2}$

N(8') - C(7') - C(11')

C(7')-C(11')-C(10') C(9')-N(8')-C(13') C(7')-N(8')-C(13')

C(7') - C(11') - C(11)

 120°

119 123 114

124

121

117

100113

110

99

106

97

111

103

114

110

109

124

115

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C(12)-C(1)-C(2)	116°
C(1) - C(2) - C(3)	119
C(2) - C(3) - C(4)	121
C(3) - C(4) - C(5)	120
$C(4) - C(5) - C(12) \dots$	121
C(5)-C(12)-C(1)	123
C(12) - C(11) - C(7)	104
C(11) - C(7) - N(6)	104
C(7) - N(6) - C(5)	109
N(6) - C(5) - C(12)	113
C(5)-C(12)-C(11)	109
C(11) - C(10) - C(9)	103
C(10) - C(9) - N(8)	106
C(9)-N(8)-C(7)	101
N(8) - C(7) - C(11)	108
C(7) - C(11) - C(10)	105
C(9) - N(8) - C(13)	117
C(7)-N(8)-C(13)	119
C(1) - C(12) - C(11)	128
C(4)-C(5)-N(6)	125
N(6) - C(7) - N(8)	111
C(12)-C(11)-C(11')	116
C(10)-C(11)-C(11')	110
C(7)-C(11)-C(11')	112
C(12)-C(11)-C(10)	109

TABLE 3	
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Standard deviations of the final atomic co-ordinates (Å)

	Atom	- (**)	- ()	- (~)	Atom	- (11)	- (1)	- (*)
	Atom	$\sigma(x)$	$\sigma(y)$	$\sigma(z)$	Atom	σ (.ε)	$\sigma(y)$	$\sigma(z)$
C(1)		0.053	0.057	0.062	C(4')	0.056	0.064	0.065
C(2)	•••••	0.060	0.059	0.061	C(5')	0.044	0.041	0.053
C(3)		0.053	0.052	0.057	C(7')	0.049	0.047	0.060
C(4)		0.058	0.053	0.059	C(9')	0.059	0.058	0.060
C(5)		0.052	0.056	0.067	C(10')	0.053	0.054	0.061
C(7)		0.054	0.053	0.062	C(11')	0.050	0.043	0.057
C(9)		0.056	0.061	0.066	C(12')	0.052	0.051	0.057
C(10)		0.052	0.052	0.054	C(13')	0.061	0.063	0.077
C(11)		0.049	0.046	0.056	N(6)	0.039	0.040	0.049
C(12)		0.043	0.042	0.059	N(8)	0.047	0.044	0.052
C(13)		0.053	0.056	0.020	N(6')	0.040	0.044	0.055
C(1')		0.048	0.050	0.064	N(8')	0.041	0.041	0.051
C(2')		0.055	0.056	0.066	Br(I)	0.006	0.006	0.002
C(3')		0.059	0.057	0.071	Br(II)	0.006	0.006	0.007

angles are consistently smaller than tetrahedral, e.g., 105° in isoclovene hydrochloride⁹ and bromodihydroisophotosantonic lactone acetate; ¹⁰ such values are consistent with the non-planarity and consequent angle deformations in cyclopentane.¹¹ Rings c and c' in chimonanthine adopt the envelope conformation with C(9) and C(9') constituting the flaps of the envelopes (see Figure 3); the angle between the mean plane through C(7), N(8), C(10), C(11) and that through C(13), N(8), C(9), C(10) is 72°, while in the other half of the molecule the corresponding angle is 64°.

The molecular arrangement in the crystal as seen in projection along the b axis is shown in Figure 3. Each of the crystallographically independent bromide ions has two contacts of less than 4 Å with nitrogen atoms. The distances involved, $N(8) \cdots Br(1)$ 4.00 Å, N(6') \cdots Br(1) 3.43 Å, N(8') \cdots Br(2) 3.18 Å, N(6) \cdots Br(2) 3.86 Å, suggest that only the contacts $N(6') \cdots Br(1)$ and $N(8') \cdots Br(2)$ represent true hydrogen bonds. The closest approach between two chimonanthine molecules is 3.27 Å and involves C(4) of the reference molecule at (x, y, z) and C(4) of the molecule at position (y, x, 1-z). A list of the intermolecular contacts of less than 4 Å is given in Table 2.

J. S. Clunie and J. M. Robertson, J., 1961, 4382.

 ¹⁰ J. D. M. Asher and G. A. Sim, Proc. Chem. Soc., 1962, 111; J., 1965, 1584.
 ¹¹ K. S. Pitzer and W. E. Donath, J. Amer. Chem. Soc., 1959, 81, 3213; F. V. Brutcher, T. Roberts, J. Bourne, M. J. Amer. Chem. Soc., 1959, 81, 3213; F. V. Brutcher, T. Roberts, J. Bourne, M. S. Bourne, S. Bourne S. J. Barr, and N. Pearson, ibid., p. 4915.



FIGURE 3. The crystal structure of chimonanthine dihydrobromide as viewed in projection along the *b*-axis

EXPERIMENTAL

Crystal Data.—Chimonanthine dihydrobromide, $C_{22}H_{28}N_4Br_2$; M, 508·3; m. p. 188—189°. Tetragonal, a = b = 13.95, c = 26.67 Å, U = 5190 Å³, $D_{\rm m} = 1.35$ g. cm.⁻³, Z = 8, $D_{\rm c} = 1.35$ g. cm.⁻³, Z = 1.35 g. cm.⁻³, 1.31 g. cm.⁻³. Space group $P4_12_12 - D_4^4$ (or the enantiomorphous $P4_32_12 - D_4^8$). Absorption coefficient for X-rays ($\lambda = 1.542$ Å) $\mu = 42$ cm.⁻¹. Total number of electrons in the unit cell = F(000) = 2064. Σf^2 (heavy atoms)/ Σf^2 (light atoms) = 2.4 at sin $\theta = 0$.

Crystallographic Measurements.—Rotation, oscillation, and Weissenberg photographs were taken with $\operatorname{Cu-K}_{\alpha}$ ($\lambda = 1.542$ Å) radiation. The unit-cell dimensions were obtained from rotation and equatorial-layer line Weissenberg photographs. The space group was determined from the systematic absences in the X-ray spectra. A small crystal, completely bathed in a uniform X-ray beam, was employed for the intensity measurements and no corrections for absorption were made. The 0kl - 9kl spectra were recorded photographically by means of an equi-inclination Weissenberg camera and the intensities were estimated visually. The usual correction factors (Lorentz, polarization, and rotation 1^2) were applied to the intensities. The various sets of structure amplitudes were placed on the same relative scale by comparison of equivalent reflexions hkl and khl; the absolute scale was obtained at a later stage by correlation with the final calculated structure amplitudes. A total of 2093 independent $|F_{o}|$ values was derived (Table 5).

Analysis of the Structure.—Three-dimensional methods were used throughout for the elucidation of the structure and the refinement of the atomic parameters.

In order to determine the positions of the two bromide ions in the asymmetric crystal unit we calculated a three-dimensional Patterson function P(UVW). Sections through this function at $W = \frac{1}{4}$, $W = \frac{1}{2}$, and $V = \frac{1}{2}$, which contain peaks representing vectors between symmetry-related bromide ions, are shown in Figure 4. We were able to assign initial coordinates to the bromide ions by consideration of these sections and of the general Patterson peaks corresponding to vectors between non-related bromide ions.¹³

The Fourier programme ¹⁴ for the DEUCE computer cannot be used conveniently for crystals belonging to the space group $P4_12_12$. To overcome this difficulty we treated the unit cell in the subsequent structure-factor and Fourier calculations as if it belonged to the

¹² G. Tunell, Amer. Min., 1939, 24, 448.

I. J. Grant, Ph.D. Thesis, University of Glasgow, 1962.
 J. S. Rollett, in "Computing Methods and the Phase Problem in X-ray Crystal Analysis," ed. R. Pepinsky, J. M. Robertson, and J. C. Speakman, Pergamon Press, Oxford, 1961, p. 87.





TABLE 4

Anisotropic temperature-factor	parameters	(b_{ij})	Х	10^{5}))
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	b_{11}	b_{22}	b_{33}	b_{12}	b_{23}	b_{13}		b_{11}	b_{22}	b_{33}	b_{12}	b_{23}	b_{13}
C(1)	661	663	182	-17	10	-700	C(4')	468	$4\overline{2}2$	196	-247	103	400
C(2)	899	627	182	-92	-2	-141	C(5')	886	753	85	-9	-216	287
C(3)	638	553	174	-60	-63	-46	C(7')	675	232	116	46	48	-195
C(4)	965	681	106	-243	-9	229	C(9')	802	858	263	13	-475	434
C(5)	551	705	143	-51	-101	921	C(10')	296	564	183	-199	82	256
C(7)	453	710	174	-58	44	-299	C(11')	577	566	191	5	131	294
C(9)	619	324	104	85	179	-73	C(12')	536	552	178	-152	18	429
C(10)	534	457	124	-39	-51	912	C(13')	266	659	123	-26	-18	301
C(11)	421	1083	217	-305	-44	-636	N(6)	415	593	182	-151	-64	155
C(12)	592	745	175	175	115	703	N(8)	487	736	101	-332	-57	396
C(13)	892	607	197	2	-4	933	N(6')	639	606	135	2	81	254
C(1')	961	274	177	-11	63	82	N(8')	541	505	128	180	-80	119
C(2')	891	885	216	-79	-49	-507	Br(I)	681	735	209	-74	-6	-89
C(3')	730	286	139	69	-172	-869	Br(II)	694	667	192	-131	-49	418

TABLE 5

Measured and calculated values of the structure factors

h	k	l	F_{o}	$F_{\mathbf{c}}$	α	h	k	l	F_{o}	F_{c}	α	h	k	l	F_{o}	$F_{\mathbf{c}}$	α
0	0	8 12 16 24 28	364 15 77 93 65	445 2 58 78 69	180 180 0 0 180			9 10 11 12 13	143 106 76 117 27	135 129 71 105 32	45 0 135 270 225			20 21 22 24 25	68 51 56 18 20	53 35 50 14 20	270 45 180 270 225
0	1	32 56 7	28 68 14 54	29 73 42 65	180 225 180 315			14 15 17 18	14 55 70 142	15 72 69 127	0 135 225 180			26 27 28 29	25 46 19 15	19 33 15 13	0 135 90 225
		9 10 11 12	10 69 184 23 191	111 186 41 176	45 0 315 270			21 22 23 24	38 18 68 28	31 14 46 23	45 180 315 90	0	6	31 32 0 1	13 13 24 79 184	14 13 20 82 174	315 270 180 135
		13 14 15 16	33 71 57 74	20 79 67 78	225 0 135 270			26 27 28 31	74 64 12 27	70 53 11 24	0 135 90 135			2345	48 36 22 42	53 54 11 34	90 225 180 135
		18 19 20 21 22	154 48 35 32 37	48 40 32 36	180 315 90 45	0	4	0 1 2 3	51 68 61 46	25 89 54 51 107	270 0 135 270 225			6 7 8 9	115 39 20 144 71	130 32 35 159	270 45 0 315 270
		23 24 26 27	63 59 37 13	60 53 30 9	315 90 0 135			4567	65 9 191 54	79 8 200 86	180 135 270 45			11 12 14 16	54 28 154 15	69 23 138 24	45 180 90 0
0	2	30 31 3 4	38 10 75 73	34 9 54 83	180 135 45 180			8 10 11 12	68 62 37 81	50 57 21 67	0 270 225 0			17 19 22 23	45 37 112 51	36 33 87 33	135 45 270 45
)6 7 8 9	290 290 186 119	249 343 214 92	270 45 180 315			14 15 17 19	177 95 63 28	183 88 54 21	90 225 135 45	0	7	26 27 2 3	22 23 118 76	15 26 120 93	90 225 180 135
		10 11 12 13	14 59 28 44	9 66 39 59	90 45 0 135			20 21 22 23	22 68 97 23	16 53 87 16	180 315 270 45			4 56 7	70 130 69 29	106 145 70 3	90 225 0 315
		14 15 17 18	79 130 97 14	92 154 75 5	90 225 135 90			24 27 28 30 31	29 35 16 21	26 25 15 23	0 225 180 90			8 9 11 12	16 65 19 24	12 46 36 25	270 45 315 270
		20 21 22 23	12 36 41 59	12 49 65 57	0 315 270 45	0	5	1 2 3 4	89 72 182 157	74 55 208 172	225 180 135 90			14 15 16 17	38 42 26 16	31 30 17 0	180 315 90 225
		24 25 27 28	16 26 15 38	14 23 2 41	0 315 225 180			56 890	107 57 48 102	83 57 40 102	225 0 270 45			18 19 20 21	32 26 25 19	27 25 18 11	0 315 270 225
0	3	29 32 1 2 4	20 14 82 18 176	29 10 80 54 191	195 180 225 180 90			10 11 13 14 15	102 33 11 11	84 74 23 19 24	315 45 0 135	0	8	28 29 30 0	22 26 14 29 129	22 22 18 34 132	90 225 0 135
		-56 7 8	95 32 101 36	97 19 76 52	45 0 135 270			16 17 18 19	42 21 106 51	54 26 90 64	90 225 180 315			2 56 7	106 68 50 160	82 72 37 143	90 315 90 225

							Тав	LE 5	(Cont	inue	d)						
h	k	<i>l</i> 9 10 11 12	F。 89 48 42 16 74	F _c 86 47 40 13 77	α 315 270 45 180	h	k	<i>l</i> 9 11 12 13 14	F。 41 38 34 48 23	<i>F</i> _c 44 41 29 46 16	α 45 135 270 45 180 270	h O	k 17	<i>l</i> 11 12 13 1 3	F ₀ 18 14 12 19 26 23	F _c 22 21 13 29 28	α 225 180 315 225 135 225
0	9	1 14 156 170 223 4 56 7 9 1 2 3 2 2 1 2 3	21 650 13 26 95 15 28 20 57 23	25220011285299208 541285299208	1)9 90 40 315 270 45 180 135 90 225 45 180 135	0	12	17 19022345234501345	57 44 27 18 32 18 32 18 39 85 88 55 88 55 825	1686052404946981	225 3150 90 1350 270 1350 270 1350 1350 1350 1350 1350 270 50 1350 270 50 50 50 50 50 50 50 50 50 50 50 50 50	1	1	57345678901123456	277 732 90 777 238 257 1531 1551 358 88	34 110 106 100 130 4 121 29 30 169 51 26 131	135 270 180 270 180 270 270 180 270 180 270
		4 5 7 0 1 1 2 3 1 5 7 1 1 2 2 3 4 1 9 0 2 2 3 4	79818150673118226221	29721546733739388	225 225 180 135 270 45 225 315 225 315 90 135 90	0	13	22312489011235778	211 32 2996 454 217 399 30 30	1773192003100282137 32363100282137	31 5 90 45 5 180 225 180 450 1350 1350 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 1355 13551155 1155 1155 1155 1155 1155 1155 1155 1155 1155 1155 1155 1155 1155 1155 11551155 11551	l	2	17023467700123456	155 955 289 21 180 580 179 580 179 274	945 1780 220 441 196 270 155 315	100 180 270 270 180 180 303 320 155 281 241 190
0 1	LO	2280135678011356 111356	13 86 96 24 114 17 29 58 37 87 21 45	12 6 120 81 43 115 8 24 42 34 75 27 56	45 270 135 45 315 90 225 180 45 135 225 0	0	14	19 20 21 2 5 6 9 10 11 13 15 1 2	20 17 20 66 25 19 38 7 41 19 17 19	19 18 16 52 00 40 29 83 1 21	315 90 225 135 270 315 270 315 270 315 275 225 135 225 180			7 8 9 10 12 13 14 15 16 17 18 9 20	42 81 75 18 145 84 59 68 53 79 53 28 24	15 77 104 13 149 86 47 75 67 59 83 54 28 25	121 276 175 64 288 17 302 16 62 74 25 202 111 261
0	11	17 190 212 23 3 4 56 7 8	26 526 23 493 493 493 297 67	23 41 32 18 26 40 28 40 28 40 28 31 75	315 225 315 315 315 315 315 30 225 315 315 315 30 315 30 315 30 315 30 315 30 30 315 30 30 30 315 30 30 30 30 30 30 30 30 30 30 30 30 30	С	9 16	345789125690 10	20 43 16 18 16 13 40 19 16 14 37 21	30 50 26 19 150 25 16 396 326	135 270 225 135 90 45 135 270 135 270 315 90	1	3	212 22 24 256 01 23 45 5	49 21 25 24 46 25 37 118 80 162 151 194	36 18 20 24 45 18 131 79 186 140 206	45 349 228 250 229 0 111 80 229 125 105

							TABLE 5 (Continued)											
h	k	l	F_{0}	$F_{\mathbf{c}}$	α	h	k	l	F_{o}	F_{c}	α	h	k	l	F_{o}	F_{c} a		
1	4	6789011235678901247012	111 71 21 140 23 526 37 38 27 88 27 72 88 27 72 84 17 49 31 275 262	94 950 1580 1383 2726 3284 3724 800 3724 800 3724 800 3724 800 3724 800 3724 3724 800 3724 3724 800 3724 3750 3724 37500 37500 37500 37500 37500 37500 37500 37500 37500 37500 37500 37500 3750	97 332 3247 3267 3550 162 131 192 154 3550 234 23150 234 23150 234 23150 234 23150 234 23150 234 23150 234 23150 234 2350 2350 2350 2350 2350 2350 2350 2350	ı	6	1457891234507901234567	24 447 381 2097 107 108 6057 107 108 1057 113	35600 36530 199979784 8860926 11229	305 200 195 114 305 31 195 163 195 163 195 217 2877 2877 2877 2877 2877 2877 2877	1	8	2222222201234567890112 1112	46 1859 1559507263804256 1994256 1994256	45 345 15 201 36 112 17 129 21 64 14 337 20 51 12 356 125 367 275 395 145 299 334 799 240 64 249 372 104 57 91		
		234567890123456789012 1121456789012	1029 2193 1228 3999 1020 1507 828 44663 809 29	10180 10	2141 21995 21955 218158 21955 2218158 2351 2555 231196 2555 2555 2555 25555 2555555555555555			-890112345678901225678	122566 1106 1107 1107 1189480 94721684157	1046659531780261409694	252605940858934495364 9440858934495364 122526005940858934495364	1	9	134567901234501234678	105 427 88 40 176 96 42 14 95 16 95 16 95 118	311 324 341 35 36 37 38 39 34 34 35 36 37 38 39 39 39 39 30 314 315 316 317 318 32 318 32 341 341 341		
l	5	2222222 222222 222222 22222 22222 22222 2222	49 31 28 230 429 62 198 600 1860 307 1337 466	4042000219576340473805 21254762473805	271 2252 1622 1900 1807 846 110 5906 551 322 203 203 203	l	7	29012345678901134567890	166 106 119 188 487 726 2890 888 442538 15290 248 442538	204 468 892 07 931 522 92 99 16	178 180 21650 21650 21650 21650 20171520 20171520 20171520 20171520	l	10	9011235678903457801345	258 284 50 50 50 50 50 50 50 50 50 50 50 50 50	26 144 25 325 98 23 45 145 19 112 42 189 41 318 39 124 39 124 39 124 39 124 39 124 30 125 15 38 24 125 15 38 24 250 15 38 24 250 16 250		

							TAE	BLE 5	(Cor	ntinue	ed)						
h	k	l	F_{0}	$F_{\mathbf{c}}$	α	h	k	l	F_{0}	F_{c}	α	h	k	l	F_{0}	$F_{\mathbf{c}}$	α
1	11	678901123469022340123	67804275110997019499	673533424411222464390	299 328 243 200 303 140 107 779 264 153 277 180 114 285	1	15	67801134568123570124	1975817522071868766037	1770 1212 1323 12132 121	202 324 111 191 351 219 26 8 26 969 26 8 281 170 26 82 2170 26 82 202 202 202 202 202 202 202 202 202			567890112345678901223	671760 476055451366449766647 1055451366449766647	98992124 1128097134856510297 1280973448556510297	40 914 55557737776 12255 231776 1806 245998 1318
		4 7 8 9 10	38 77 50 22 56	45 86 42 24 42	137 250 320 357 32	1	16	15 1 2 4 5	13 14 12 15 13	17 13 12 19 22	209 193 260 268 26			24 25 26 27 29	16 29 18 31 17	19 36 15 34 17	24 300 22 123 275
1	12	11 12 14 156 17 18 19 0 1 2 3 4 56 7	4223252223833242924 2325222383326242924	422325221383262464	5399051295330045553201291212105121212121212121212121212121212121	1	17 2	012370123456789012	10 16 11 18 532 206 11 282 166 32 122 366 432 123 16 432 123 10 123 10 10 10 10 10 10 10 10 10 10 10 10 10	181 974 2241 530 19530 2555 2154 22710 2010	180 345 299 179 52 270 270 270 180 180 90 180 90 180 90	2	4	30012345678901123456	12 111 120 44 206 1023 44 206 1023 556 60 944 1026 1202 556 0394 1202 120	19 85 54 50 29 59 10 9 88 55 10 55 10 55 10 7 88 55 10 7 88 55 10 7 88 55 10 7 88 55 10 7 88 55 10 7 9 7 88 55 10 7 9 7 9 7 9 7 9 7 9 7 9 7 9 7 9 7 9 7	2530 29666 29666 29332 34864 94346 2566 2566 2943 2566 2566 2566 2566 2566 2566 2566 256
1	13	90156012345670	5154988851239524 28288851239524	+288327574170850	229 179 265 102 196 211 72 120 241 57 241			13 14 15 16 7 8 91 22 25 6 90	71 399 497 448 1312 417 254 2547	106 180 21 354 1352 3258 2007	90 180 270 180 90 180 270 270 270 0 270 0 270 0 90			17 18 19 21 22 24 56 78 90 22 28 90	260 292 421 604 261 254 254 280 254 280 254 280 254 280 254 280 254 280 292 292 292 292 292 292 292 292 292 29	18 21 24 46 55 56 81 26 24 24 24 24 24 24 24 24 24 24 24 24 24	103 112 101 202 259 305 91 277 146 342 181 382
1	14	14 0 1 2 3 4	59 17 15 17 21 15	64 24 18 18 25 19	270 0 116 330 186 275	2	3	31 0 1 2 3 4	23 140 158 23 136 82	24 121 181 50 198 93	90 246 176 56	2	5	012345	25 57 85 93 49	9 59 84 89 81 41	180 276 148 74 161 187

					Тав	LE 5	(Cont	inued)						
h	k	l	F_{0} $F_{\mathbf{c}}$	α h	k	l	F_{0}	$F_{\mathbf{c}}$ a	h	k	l	F_{o}	$F_{\mathbf{c}}$	α
		6 7 8 90 10 11 12 13 14 15 16 17 18 19	104 75 3 68 47 5 84 78 2 81 77 7 72 63 3 154 136 2 171 136 2 31 27 1 54 64 10 76 78 1 63 59 1 35 35 1 39 30	59 165 28 52 55 55 55 59 00 6 76 5 5 76 5 5 5 5 76 5		10 11 12 14 16 17 18 20 21 23 24 25	49 83 35 43 56 80 22 80 22 80 22 20	41 282 58 266 59 336 32 148 47 130 41 165 27 316 41 48 57 249 12 305 23 253 26 127 21 12 22 280	2	10	24 22 27 0 1 2 3 4 5 6 7 8 9	19 21 22 12 34 5 40 76 70 84 5	21 2250 40531 4371 85732	39 358 140 199 200 13 92 289 108 174 244 52
2	6	1222222222 20123456800123456789022	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2 931 2533 2959 9958 917 888 818 366 76 76 76 76 76 76 76 76 76 76 76 76 7	8	228012345678901124569010	249983960234966055572792 12529732844966055572792	$\begin{array}{c} 26 \\ 114 \\ 14 \\ 78 \\ 15 \\ 136 \\ 174 \\ 67 \\ 71 \\ 19 \\ 14 \\ 73 \\ 14 \\ 73 \\ 14 \\ 26 \\ 188 \\ 194 \\ 269 \\ 12 \\ 348 \\ 269 \\ 12 \\ 348 \\ 269 \\ 12 \\ 348 \\ 269 \\ 12 \\ 365 \\ 11 \\ 326 \\ 11 \\ 10 \\ 10 \\ 10 \\ 10 \\ 10 \\ 10 \\ 1$	2	11	10 11 12 14 16 790 22 0 12 34 56 780	22455122456767883398	222123245874573525295728806	181 57 219 960 220 78 3214 332 70 139 71 3277 212 151 558
2	7	1345678901245678900123456789	$\begin{array}{c} 40 & 29 & 5 \\ 99 & 101 & 3 \\ 26 & 37 & 6 \\ 31 & 28 & 16 \\ 18 & 21 & 28 \\ 29 & 28 & 22 \\ 15 & 18 & 15 \\ 22 & 28 & 15 \\ 12 & 28 & 15 \\ 12 & 28 & 16 \\ 19 & 20 & 15 \\ 12 & 28 & 16 \\ 19 & 20 & 16 \\ 19 & 20 & 16 \\ 19 & 20 & 16 \\ 19 & 20 & 16 \\ 19 & 20 & 16 \\ 19 & 20 & 16 \\ 19 & 20 & 16 \\ 19 & 20 & 16 \\ 19 & 20 & 16 \\ 19 & 20 & 16 \\ 19 & 20 & 16 \\ 19 & 20 & 16 \\ 10 & 68 & 16 \\ 10 & 65 & 20 \\ 106 & 80 & 20 \\ 106$	16777284688905512005560260449673	9	2234567123456789023456789023	2270994799224146062227679991099 1278386242548227679991099	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2	12	10 11 13 14 15 67 90 11 23 02 34 56 78 90 11 23 4 11	4522213210830524384637048545	55221611788298198972119628399584281	2499 1399 901 122 242 214 3355 240 295 180 295 2320 272 132 295 2320 272 1152 60 241 295 2320 272 1152 60 241 291 291 291 291 291 291 291 291 291 29

							TAB	LE 5	(Con	tinuec	d)						
h	k	l	F_{o}	F_{c}	α	h	k	l	F_{o}	$F_{\mathbf{c}}$	α	h	k	l	F_{0}	$F_{\mathbf{c}}$	α
2	13	15 16 17 19 20 21 0 1 2 3	21 38 23 16 21 37 22 33 29	22 40 22 28 16 19 41 19 38 26	272 106 276 276 276 297 0 168 81 5	3	4	18 19 20 21 23 26 27 29 0 1	100 73 20 16 71 27 48 22 126 51	103 89 13 73 30 55 16 125 104	180 90 180 270 270 270 90 270 90 293	3	6	0123456789	107 84 85 86 124 983 56 98 68	122 88 66 99 137 109 77 37 88 80	0 268 173 280 98 97 305 4 204 . 88
		4 5 8 10 11 12 13 16 17 18	68 41 28 27 17 27 26 21 14	60 38 38 37 28 29 29 23 17	254 343 123 318 103 69 138 230 233 192			2 3 4 56 7 8 9 0 1 11	67 102 152 93 76 32 45 43 90 85	48 118 153 87 54 38 53 66 106 88	328 156 107 165 268 98 136 210 331			10 11 12 13 14 15 17 18 20 21	56 24 82 46 19 58 48 17 16	50 24 82 81 51 33 69 48 12 15	182 128 277 285 81 41 249 35 .124 77
2	14	19 1 2 4 56 7 80 12	23 18 48 17 15 19 17 17 28	25 18 62 16 19 27 14 28 28 28	303 37 288 234 222 248 358 315 105			12 13 14 15 16 17 18 19 20	115 43 60 37 54 42 27	120 450 586 367 371 371	304 298 139 83 235 355 4 88 142 130	3	7	22345601234	15 34 29 22 35 10 51 40 31	11 26 31 19 24 55 50 26	211 258 35 33 130 251 73 39
2	15	10 12 34 58 910 11	16 180 24 36 17 156 20	12 15 19 33 24 19 15 29 20	180 175 97 143 242 273 40 326 324 326 324	3	5	22 23 25 27 0 1 2 34 5 27 0	27 49 29 19 57 83 579 579	25 40 48 20 82 80 80 81 89 80	306 239 58 216 131 42 71 242 65 7			4567890 10112 1314	86 99 21 44 38 65 95 115 64 51	89 89 29 24 31 55 71 95 70 46	354 207 40 253 170 321 326 206 181 45
2	16	2023456	14 17 14 15 12	18 23 15 23 24	180 300 189 299 159			6 7 8 9 10	69 64 41 48 84 36 80	19 68 36 44 86 41 67	189 49 208 252 356 308			15 16 17 18 19 20 21	40 24 28 65 64 30	55 18 52 43 28 37	48 45 195 178 292 7
3	3	100123456780	18 171 88 73 85 17 245 76 22 97	9 188 92 53 99 44 230 80 109	132 90 270 180 90 180 270 180 270			12 13 14 15 16 17 18 19 22 23	1032 400 4598 4575 6737 27	95651270587	197 210 62 198 2 77 183 118 15 262	3	8	223456780123	31 41 28 17 24 20 18 137 43 113 88	-56 366 223 167 139 304 104 104	298 356 134 245 19 107 328 137 271
		1Ó 13 16 17	46 97 24 63	-66 99 5 73	270 90			24 25 26 27	34 26 39 22	29 23 35 23	125 254 42 290			/4 56 7	37 64 83 44	34 71 81 43	110 143 358 73

							TAE	BLE 5	(Con	tinued)					
h	k	l	F_{0}	F_{c}	α	h	k	l	F_{o}	$F_{\mathbf{c}}$ a	h	k	l	F_{o}	F_{c} a
3	9	80134567901234567012345673	8683554328936007527369384987	7567756035527888853412266883025 893756254305527888853412266883025	191 309 114 10 279 2279 2255 235 58 850 388 191 882 239 2274 9 2357 8850 388 191 882 239 2274 9 2274 9 2274 2375 2275 2275 2275 2275 2275 2275 2275	3	12	4 56 7 8 901123567 8 901 1123567 8 901 1123567 8 901	752625193138985796710553092	$\begin{array}{c} 73 & 102 \\ 60 & 354 \\ 28 & 262 \\ 21 & 243 \\ 22 & 212 \\ 24 & 245 \\ 24 & 245 \\ 24 & 245 \\ 24 & 245 \\ 24 & 247 \\ 23 & 269 \\ 21 & 240 \\ 23 & 269 \\ 21 & 240 \\ 23 & 269 \\ 21 & 240 \\ 23 & 269 \\ 23 & 260 \\ 24 & 240 \\ 24 &$	3	16	45679010135789012345678901	163236 16423745601 18517700 14676649 160115049	$\begin{array}{cccccccccccccccccccccccccccccccccccc$
3	10	80123456891223023456890	87570306978874025632311	852481072793247455192622	299 16 195 294 195 294 195 195 195 2754 162 2651 1377 183 184	3	13	11 12 14 16 17 18 90 12 34 57 890 11 14	42304186963559225232890221	47 260 29 39 46 37 24 21 14 11 14 21 27 87 47 21 23 24 24 21 14 11 14 21 23 28 24 21 24 21 24 21 25 81 24 21 29 81 21 22 23 29 28 52 80 21 21 21 21 21 21 21 21 21 21 21 21 21	4	5	11234567890123567890123	2316623628339752384683	$\begin{array}{cccccccccccccccccccccccccccccccccccc$
3	11	11 12 13 14 15 16 18 19 21 23 0 1 23 0 1 23	59 571 29 20 20 20 20 20 20 20 20 20 20 20 20 20	4654996789819924	53 51 91 330 164 263 2271 130 83 2353	3	14	15 18 19 20 0 1 26 7 8 11 16 7 0 1	272520680580740 1220680580740	$\begin{array}{cccccccccccccccccccccccccccccccccccc$			4567890112345678 10112345678	102 24 588 93 30 981 524 43 71 53	112 2 ¹ / ₂ 5 20 87 59 349 76 31 87 240 37 254 81 264 84 55 28 84 48 1386 77 101 26 26

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							Тав	LE 5	(Con	tinue	d)						
h	k	l	F_{o}	F_{e}	α	h	k	l	F_{o}	$F_{\mathbf{c}}$	α	h	k	l	F_{o}	F_{ullet}	ά
		19 20 21 23 24 256 27 28 20 30	38 51 26 18 53 28 17 18 11 28 11	32 41 27 16 22 33 19 15 28	91 237 343 182 272 310 280 135 271 225 119	4	8	2245670123454	22 32 23 23 23 23 23 23 23 23 26 32 63 26 4 26 4	2790 222 24 5766 371	236 325 314 154 306 196 90 127 61 174			9 10 11 12 14 15 16 17 18 19 20	62 21 42 16 34 45 16 321 36 20	70241 1286 540 16 551 21	134 238 15 285 30 81 291 242 279 76
4	6	0123456789011234	126 9430 991 991 991 991 995 102 54 86 337 44	1606 999 40 816 9294 5274 5274 547	54 180 208 62 196 39 122 178 178 347 35 335 290 138 307			67801123456890135	106 731 8 74 79 8 2 32 4 74 79 8 2 35 7 4 5 74 5	102560424290878630	111 195 280 1317 253 62 96 201 277 88 207 1288 207	4	11	2230123567890114619	20 18 21 92 46 92 84 45 24 23 22 28 45 22 28	14187750230 5023183283 243183283 2483283 2483	2130 2130 643 282 131 245 9322 1380 2270 270
4	7	14 5678901234567801234	44 65 71 11 23 19 18 22 18 12 16 14 53 17	334 811 322 313 138 20 89 123 3 513 337 67	1 33 105 159 65 211 100 317 245 215 215 215 40 150 43 129 105 240	4	9	206801234567901234567	106688378111898604698	204 14 3 2 1 9 3 4 4 9 0 6 6 6 7 6 9 6 4 7 6 7 1 9 3 4 4 9 0 6 6 6 7 6 9 6 4 7 6 7 1 9 7 4 9 7 6 7 1 9	2078 888 180 57 191 231 231 231 232 191 232 232 192 232 193 2766 231 2951 2951 2951 2951 2951 2951 2951 295	4	12	192123456789011236790112167901	188522685986902800883	14485341264452308850146771662	29173263145039033336625 221112836425
		6789011234 1121341561789021	550774 776799263770312518	398476077606 2327586024 18	316 32 239 251 249 331 117 282 112 88 94 233 26	4	10	18012345601234568	380 1516 1736 235 345 5384 5498 5498	43129203656351412 223535566	8 171 141 292 118 93 23 14 311 52 134 84 265 122 265	4	13	22 0 1 2 4 56 7 90 11 137 18 90	136 21 21 21 22 20 256 255 13	12637719953135150	86 0 113 89 283 128 257 161 295 73 179 488 193 43

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The Structure of Chimonanthine

						TA	BLE 5	(Con	tinue	d)						
h	k	l	F_{o}	$F_{\mathbf{c}}$ a	ļ	, /	k l	F_{o}	F_{c}	α		h k	l	F_{0}	$F_{\mathbf{c}}$	α
4	14	124 56780	15 23 17 32 21 25 17	18 32 30 32 26 17 37 18 23 19 26 18 32	937 1500		16 17 18 19 20 22 23 24	28 47 50 26 29 26	34 49 36 27 29	231 175 345 28 162 167 282 54			9 10 11 13 14 15 16 17	45 32 31 40 48 24 19 24	33 39 26 34 57 26 10	78 130 250 162 89 90 93
4	15	11 12 13 1 4 5 7	18 23 21 20 21 17 15 12	24 13 29 21 23 11 23 24 18 33 17 27 16 35	18635555	7	267012345	20 17 21 76 62 106 63 70	20 20 91 53 105 71 59	132 193 180 267 328 61 59 305	5	10	20 21 22 0 1 26 7	24 20 31 26 84 28 53	267 39558 787 53	288 106 273 180 70 139 275 117
4	16	11 12 13 1 2 5	20 18 20 12 12 15 23	27 32 24 2 27 16 8 7 19 2 23 19 34 17	6 3 4 2 1 7 0		6 7 9 10 11 12	43 61 37 21 43 61	31 72 39 53 18 38 58	177 71 256 118 200 250 210			8 9 10 12 13 14 15	30 40 94 27 27 44 53	39 31 86 25 36 44 54	18 232 315 36 78 102 287
5	5	701234678	15 12 54 15 78 105 94 97 54	15 31 7 54 27 13 18 68 9 112 84 18 90 9 64 18	6 0 0 0 0 0 0 0 0 0 0		13 14 16 18 20 21 23 24 25	27 78 43 19 40 23 24 19 18	34 65 42 18 38 21 20 18 23	228 77 22 16 348 51 357 176 305	5	11	17 18 21 23 0 2 3 4	25 54 28 26 18 47 44 44	25 52 32 17 14 55 38	72 171 235 235 68 0 280 37 107
5	6	9 10 11 12 13 14 15 16 17 18 190 24 5 0	14 42 71 102 49 78 22 41 34 42 41 67 42 47 112 5	14 9 55 27 88 18 54 27 72 27 531 9 356 18 44 9 41 18 430 120 20	000000000000000000000000000000000000000	8	26 27 0 1 2 3 4 5 6 7 8 9 0 11 12 3	206 24 25 74 25 74 47 30 35 53 1 29 20 41 75 21 20 20 20 20 20 20 20 20 20 20 20 20 20	17726151186285966 24483265966	301 73 289 152 293 99 50 95 237 298 50 237 298 144 28 206 144 28 29 206 147 29 206 237	5	12	5678913469010123	350 339 297 49 191 205 244 24 310	33332332412959396	243 314 237 238 192 341 100 11 293 1350 188 118 188
		1234567890112345	7708899446587558	2-6 129 763 88 20 111 879 8 10 111 879 8 10 111 879 8 10 11 172 546 16 29 11 172 546 16 29 27 11 172 546 29	519558693699809	9	1457122501234568	23944537066030303260303	2434332170265309	2882 21095 2476 2520 281 3055 81 3576 244	5	13	7456789012345780	176 240 419 35 58 200 72 33 33 33 33 33	351872268057480 368723413057480	970 2709 1769 219 313 303 70 25 322 19 176 0

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Grant, Hamor, Robertson, and Sim:

							Тав	LE 5	(Cont	inued	d)						
h	k	l	F_{0}	$F_{\mathbf{c}}$	α	h	k	l	F_{0}	F_{c}	α	h	k	l	F_{o}	F_{c}	α
		1 34 57 8 91 136 17 18 19	30 27 23 21 26 48 26 31 21 21 11 15	290 24 21 25 28 31 25 28 31 25 31 25 37	79 77 227 211 272 209 311 213 21 56 154 159 52	6	8	21 22 250 12 34 56 78	19 22 22 20 38 24 50 45 49 47	1392199752256911 224625691	279 256 171 213 180 347 134 125 91 332 2332	6	11	220123456781123	18 31 44 54 29 19 27 35 29	21 35 45 21 52 25 22 23 18	89 0 119 37 326 340 66 196 238 206 93 166 280
5	14	1 2 56	33 33 25 21	42 35 21 24	174 18 303 172			9 10 11 12	50 64 72 28	50 57 58 33	162 331 294 220			14 16 17 22	28 21 17 18	27 34 16 15	54 10 348 307
5	15	7 0 1 5	36 24 21 22	42 36 24 26	168 0 345 243			13 14 15 16	66 27 44 24	66 22 45 26	268 292 23 49	6	12	23 1 2 3	11 48 19 27	15 56 17 29	345 340 157 323
6	6	803567	19 127 43 51 21	25 156 39 58 2 33	165 180 90 90 180 270			17 18 20 21 22 23	29 30 18 47 21 23	22 30 17 43 22 25	25 194 320 90 147 268			4 6 7 9 11 12	47 21 40 30 24 28	40 23 41 37 23 32	100 35 351 139 155 315
		8 10 11 12 13 14 15 16 18 19 20	678884277886 2778659	60 60 81 93 81 93 81 34 30 18	270 270 270 90 180 180 90 180	6	9	1 2 3 4 56 7 90 10 11 12	12620553840469	20 57 6 18 9 13 6 11 5 20 7 6 18 9 13 8 11 5 20 7 6	91 13 273 48 113 263 151 257 216 49 231	6	13	13 14 3 4 5 6 90 11 23	25 23 23 23 23 23 23 24 20 17 21 18 25	27 22 22 37 22 37 24 24 29 21 20 30	185 185 247 185 247 185 172 356 131 179
6	7	21 22 23 24 25 0 1 2	40 31 71 23 28 42 21	41 231 16 18 256 20	90 180 270 180 270 0 332 275			14 15 16 18 19 20 21 22	304 324 324 255 34 255 34	368861555	120 328 358 125 26 190 295	6	14	14 1 2 5 7 8 10 11	20 27 21 20 16 15 21	21 31 17 21 22 24 13 21	25 12 151 137 50 306 157
		3456790 10	45 15 63 85 73 43	54 12 49 58 76 72 46	212 327 129 304 69 254 172	6	10	0123468	52 65 399 730 47	51 69 34 51 78 48 41	0 342 120 67 88 37 204	6	15	12 13 0 2 5 6 7	24 22 15 18 16 20 14	34 24 16 26 17 21	339 7 297 340 235 191
		11 12 13 14 15 17 18 19 20	88 20 52 57 27 44 16	77 18 35 58 59 20 41	5 73 340 121 257 48 349 133 197			9 10 11 12 13 14 15 20 21	48 19 223 40 28 22 22	47 15 22 17 18 39 24 19	253 218 296 299 251 85 274 124	7	7	801235679	15 257 30 970 962 30 71 80	19 159 129 31 894 260 68	242 180 270 90 270 180 90 90

							TAE	BLE 5	(Con	tinue	d)						
h	k	l	F_{0}	F_{c}	α	h	k	l	F_{0}	$F_{\mathfrak{e}}$	α	h	k	l	F_{0}	$F_{\mathbf{c}}$	α
7	8	10 11 12 14 16 18 0 2 3 4 5 6 7	56 48 226 78 591 240 46	597 591 334 792 877 587 640	180 270 180 0 180 86 330 245 35 50	7	12	13 15 16 17 8 90 21 0 1 2 3	44 27 42 24 17 20 57 20 316 27	52 34 22 27 42 25 60 43 27 27 42 32 32	359 202 302 359 202 350 200 200 200 200 200 200 200 200 200 2	8	10	13 14 15 0 2 4 56 7 8 910	26 326 26 26 26 26 27 26 27 27 27 27 27 27 27 27 27 27 27 27 27	314 324 2251 527 5366 23	342 73 359 162 127 257 17 313 171 192 187
7	9	7892345789213567	526224077058383255	534824600965412	89 337 136 172 254 134 254 254 254 254 263 263 263 286 286 286 286 29 286 286 29 286 286 29 286 29 20 20 20 20 20 20 20 20 20 20 20 20 20	7	13	5 67 89114579012458	32239963040409255	3212332534711776864	318 166 1831 3229 3336 134 008 256 203	8	11	11 13 14 19 13 4 56 71 20 12	52623317092293262296 223213329293266296	574771033387632373253374	253 2730 22347 2602 139 151 190 151 190 158
7	10	8901123415678900123	476847654917379208	474 667 4 3 3 2 2 4 5 1 6 97 6 3 0 4 3 0 4 5 1 6 97 6 3 0	326 60 174 215 10 311 136 31 118 241 19 308 241 19 308 229 123 336	7 3	14	90235012346781236	183227094 2212294 247224 25778 2578	2224322222333216930	203 205 53 355 180 151 345 103 147 195 270 180 90	8 9	13 9	46712024689001545	28 253 251 223 251 224 23 251 259 69 922 68	279065817963457256 21796345743156	84 18 192 299 180 248 17 159 250 116 7 180 270 180 90
7	11	4568011357805689112	54824002226887232417 1872332417	222542548552243335 222542548552243335 2542548552243335	281 66 349 311 227 92 158 0 160 344 281 194 42	8	9	901125810123456782	534233165161579598	44414246334643605	90 180 270 90 90 180 132 16 267 60 108 207 169 40 194	9	10	67891123456780124	7795053885494648063	630552746917746969	0 90 90 270 180 270 180 270 180 180 180 180 188 114 272

							TAI	BLE 5	(Con	tinued	l)						
h	k	l	F_{o}	F_{e}	α	h	ł	e l	F_{o}	$F_{\mathbf{c}}$	α	h	k	l	F_{0}	$F_{\mathbf{c}}$	α
9	11	56789012345689023	467292853206306098	32232 151875525194	36 150 344 319 222 13 148 229 60 1252 314 172 282	9	12	4 56 7 12 14 56 80 2 56 7	258238025118904134239	27 348 20 18 27 24 27 19 537 28 30 28 30 36	266 207 551 207 551 355 180 315 315 3200 250	9	13	8911214 15723456790 11	356 202 125 14 197 156 215 26 21 26 21 14	235752179774614192 111122143192	5 163 309 136 61 27 131 2748 150 34 235 277 91

orthorhombic space group $P2_12_12_1$, with two molecules in the asymmetric crystal unit. This change involves a shift of the origin to $(\frac{1}{4}, 0, \frac{3}{8})$.

The first set of structure amplitudes and phase angles was calculated on the basis of the bromide ions alone; the value of R, the average discrepancy between measured and calculated structure amplitudes, was 39.9%. With the measured |F| values and the calculated phase angles we then evaluated a three-dimensional electron-density distribution and displayed it as contoured sections drawn on sheets of glass and stacked in a frame. From this electron-density distribution we were able to assign co-ordinates to all the carbon and nitrogen atoms in the molecule and to establish structure (V) for the dihydrobromide of chimonanthine.

Each atom was allotted an isotropic temperature factor B of 4.5 Å^2 and a second set of structure factors was calculated. The value of R decreased to 29.3%.

Three further rounds of Fourier and structure-factor calculations served to reduce the value of R to 19.1%.

The analysis was completed by means of two cycles of least-squares adjustment of positional and thermal atomic parameters. The programme devised by Rollett ¹⁴ was employed. The value of R fell to 14.9%. The final values of $|F_0|$, $|F_c|$, and α are shown in Table 5. The theoretical atomic scattering factors used in the structure-factor calculations were those of Berghuis et al.¹⁵ for carbon and nitrogen and the Thomas-Fermi ¹⁶ values for bromine.

The final atomic co-ordinates, molecular dimensions and some non-bonded distances are given in Tables 1 and 2. The standard deviations of the final atomic co-ordinates were derived from the least-squares residuals by means of the equation:

$$\sigma^2(x_i) = \sum_j \omega_j \; (\Delta F_j)^2 / [(n - s) \sum_j \omega_j \; (\partial F_j / \partial x_i)^2].$$

The results are listed in Table 3. The parameters defining the anisotropic thermal vibrations are listed in Table 4; they are values of b_{ij} in the equation:

$$\exp(-B\sin^2\theta/\lambda^2) = 2^{-(b_{11}h^2 + b_{22}k^2 + b_{33}l^2 + b_{12}hk + b_{23}kl + b_{13}hl)}.$$

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¹⁸ J. Berghuis, J. M. Haanappel, M. Potters, B. O. Loopstra, C. H. MacGillavry, and A. L. Veenendaal, Acta Cryst., 1955, 8, 478. ¹⁶ "Internationale Tabellen zur Bestimmung von Kristallstrukturen," Borntraeger, Berlin, 1935,

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